A cortical sparse distributed coding model linking mini- and macrocolumn-scale functionality

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INTRODUCTION

The columnar organization of neocortex at the minicolumnar (20–50 µm) and macrocolumnar (300–600 µm) scales has long been known (see Mountcastle, 1997; Horton and Adams, 2005 for reviews). Minicolumn-scale organization has been demonstrated on several anatomical bases (Lorente de No, 1938; DeFelipe et al., 1990; Peters and Sethares, 1996). There has been substantial debate as to whether this highly regular minicolumn-scale structure has some accompanying generic dynamics or functionality. See Horton and Adams (2005) for a review of the debate. However, thus far no such generic function for the minicolumn — i.e., one that would apply equally well to all cortical areas and species — has yet been proposed. I propose that the minicolumn does have a generic functionality, which only becomes clear when seen in the context of the function of the higher-level, subsuming unit, the macrocolumn. I propose that: (a) a macrocolumn's function is to store sparse distributed representations of its inputs and to be a recognizer of those inputs; and (b) the generic function of the minicolumn is to enforce macrocolumnar code sparseness. The minicolumn, defined here as a physically localized pool of ~20 L2/3 pyramidal, does this by acting as a winner-take-all (WTA) competitive module, implying that macrocolumnar codes consist of ~70 active L2/3 cells, assuming ~70 minicolumns per macrocolumn. I describe an algorithm for activating those codes during both learning and retrievals, which causes more similar inputs to map to more highly intersecting codes, a property which yields ultra-fast (immediate, first-shot) storage and retrieval. The algorithm achieves this by adding an amount of randomness (noise) into the code selection process, which is inversely proportional to an input's familiarity. I propose a possible mapping of the algorithm onto cortical circuitry, and adduce evidence for a neuromodulatory implementation of this familiarity-contingent noise mechanism. The model is distinguished from other recent columnar cortical circuit models in proposing a generic minicolumnar function in which a group of cells within the minicolumn, the L2/3 pyramidal, compete (WTA) to be part of the sparse distributed macrocolumnar code.

Keywords: sparse distributed representations, minicolumn, macrocolumn, novelty detection, population coding, learning, memory, winner-take-all

No generic function for the minicolumn — i.e., one that would apply equally well to all cortical areas and species — has yet been proposed. I propose that the minicolumn does have a generic functionality, which only becomes clear when seen in the context of the function of the higher-level, subsuming unit, the macrocolumn. I propose that: (a) a macrocolumn's function is to store sparse distributed representations of its inputs and to be a recognizer of those inputs; and (b) the generic function of the minicolumn is to enforce macrocolumnar code sparseness. The minicolumn, defined here as a physically localized pool of ~20 L2/3 pyramidal, does this by acting as a winner-take-all (WTA) competitive module, implying that macrocolumnar codes consist of ~70 active L2/3 cells, assuming ~70 minicolumns per macrocolumn. I describe an algorithm for activating those codes during both learning and retrievals, which causes more similar inputs to map to more highly intersecting codes, a property which yields ultra-fast (immediate, first-shot) storage and retrieval. The algorithm achieves this by adding an amount of randomness (noise) into the code selection process, which is inversely proportional to an input's familiarity. I propose a possible mapping of the algorithm onto cortical circuitry, and adduce evidence for a neuromodulatory implementation of this familiarity-contingent noise mechanism. The model is distinguished from other recent columnar cortical circuit models in proposing a generic minicolumnar function in which a group of cells within the minicolumn, the L2/3 pyramidal, compete (WTA) to be part of the sparse distributed macrocolumnar code.

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Hetherington and Swindale, 1999; Ringach, Favorov and V1 orientation columns (characteristics, or tuning, by the cells comprising the minicolumn, e.g., have been suggested is possession of highly similar receptive field features, or tuning, by the cells comprising the minicolumn, e.g., V1 orientation columns (Hubel and Wiesel, 1962, 1968) and minicolumn-sized regions innervating cutaneous zones (Favorov and Diamond, 1990). The reasoning here appears to be that because a group of cells all have very similar tuning to a particular feature, e.g., an edge at a particular orientation, they form a unit whose function is to recognize α. However, in searching for a possible generic minicolumnar function, we need not limit ourselves to considering only recognition functions. Furthermore, possession of highly similar tuning cannot be a basis for a generic minicolumn functionality since in many cortical areas, the cells encountered along vertical penetrations can have quite variable tuning (cf. Sato et al., 2007, 2008). On closer analysis, this is true in orientation column data as well (Hetherington and Swindale, 1999; Ringach et al., 2002). If there is a generic minicolumnar functionality, then it must be compatible with varying degrees of tuning correlation amongst the minicolumn's cells.

I propose that the minicolumn does have a generic functionality (given shortly), but one that only becomes clear when seen in the context of the function of the higher-level, subsuming unit, namely, the macrocolumn, which has been demonstrated anatomically (Goldman and Nauta, 1977; Lübke et al., 2003; Egger et al., 2008) and functionally (Mountcastle, 1957; Woolsey and Van der Loos, 1970; Hubel and Wiesel, 1974; Albright et al., 1984). I propose that the function of a macrocolumn (e.g., hypercolumn, segregate, barrel) is to store sparse distributed representations of its overall input patterns, and to act as a recognizer of those patterns. By “overall input” pattern, I mean the macrocolumn's overall input at a given moment, including not only its bottom-up (BU) inputs from thalamus or lower cortical areas, but also its top-down (TD) inputs from higher cortical areas and its horizontal (H) inputs, which I propose carry temporal (sequential) context information (recurrently) from the representations previously active in the same and nearby macrocolumns. Thus, an “overall input pattern” can equally well be termed, a “context-dependent input”. Thus, it is in fact the macrocolumn whose generic functionality is appropriately characterized as recognition; i.e., recognition of a class determined by the history of context-dependent inputs to which it has been exposed.

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A distributed representation of an item of information is one in which multiple units collectively represent that item, and crucially, such that each of those units generally participates in the representations of other items as well. Distributed representations are also referred to as cell assemblies, population codes, or ensembles. In this paper, “representation” and “code” will be used interchangeably. A sparse distributed code (SDC) is one in which only a small fraction of the pool of available representing units is part of any particular code (Palm, 1982; Lynch et al., 1986; Kanerva, 1988).

If the macrocolumn stores SDCs, then there must be some mechanism that enforces sparseness and this, I propose, is the generic function of the minicolumn. Specifically, I propose that small, physically localized pools of L2/3 pyramids, e.g., ~20 such cells, act as winner-take-all (WTA) competitive modules (CMs). This implies that macrocolumnar codes should consist of about 60–80 active L2/3 cells, one per minicolumn: for simplicity, assume 70 minicolumns per macrocolumn hereafter. Defined in this way, the minicolumn has a more flexible relation to the ontogenetic column, the apical dendrite bundle, the DBC, horsetail, etc. For example, a given minicolumn might include L2/3 pyramids from more than one apical dendrite bundle, consistent with the findings of Yoshimura and Callaway (2005) of fine-scale networks of preferentially interconnected L2/3 pyramids.

There is increasing evidence for the use of SDC in the cortex and other brain structures; e.g., auditory cortex (Hromdka et al., 2008), visual areas (Young and Yamane, 1992; Vinje and Gallant, 2000; Waydo et al., 2006; Quian Quiroga et al., 2008), zebra finch neopallium (Hahnloser et al., 2002), olfactory structures (Jortner et al., 2007; Linster and Cleland, 2009; Poo and Isaacson, 2009), and hippocampus (Leutgeb et al., 2007). Particular supportive of the proposed hypothesis is the Reid Lab’s calcium imaging data of rat V1 during stimulation by drifting square-wave gratings (Ohki et al., 2005). Their movie (http://reid.med.harvard.edu/movies.html) shows sparse collections of L2/3 cells extending over an approximately macrocolumn-sized region synchronously turning on and off in response to particular grating orientations. Figures 1A,B (two frames from the movie) show distinct sets of cells, i.e., codes, responding to bars moving left and right, respectively, and emphasize that individual units may participate in multiple codes (red-circled cells). In terms of the proposed model, the active neurons would be the winners in their respective minicolumns, as suggested in Figures 1C,D. Figure S1 in Supplementary Material provides another view of how the proposed model maps onto cortex.

If the macrocolumn does indeed function as a SDC field in the way suggested here, then we must answer two key questions regarding its dynamics.

1. How is any particular set of winners, one in each of the 70 minicolumns, initially chosen in response to an input pattern and bound into a holistic code? That is, how are macrocolumnar codes learned?
2. How is a previously learned code reactivated in response to future presentations of the input pattern that it was initially chosen to represent? That is, how are stored macrocolumnar codes retrieved (reactivated)?

In the next section, I describe an algorithm, referred to as the code selection algorithm (CSA), which answers both questions. A key property of the CSA is that it causes similar inputs to be assigned to similar, i.e., more highly intersecting, codes. This property, which will be referred to as SISC (similar inputs map to similar codes), is very important in terms of computational efficiency (see Discussion) and is possessed by most distributed coding schemes. However, the CSA achieves it in a novel, probabilistic fashion, which can be summarized as follows:

1. Determine the familiarity of a macrocolumn’s input. To a first approximation, an input’s familiarity is its maximum similarity to any input previously stored in the macrocolumn.
2. Set the amount of randomness (noise) in the process of selecting winners in the WTA modules in inverse proportion to the input’s familiarity.
3. Select the winners.

The algorithm’s rationale is described in detail in the next section, but broadly, the idea is as follows. When an input, \( \alpha \), is familiar, we want to reactivate the code, \( \beta_1 \), to which \( \alpha \) was
progress in understanding many of the components of cortical circuitry, and more specifically, the putative canonical cortical microcircuit (Rockland and Pandya, 1979; Douglas et al., 1989; Douglas and Martin, 1991). I therefore want to finish the Introduction with the following point. We have made huge strides in understanding how cortical columnar circuitry manipulates, i.e., stores and retrieves, specific items of information. In the main, only very broad conclusions regarding information processing are asserted in the experimental literature, e.g., horizontal connections between fast-spiking L4 interneurons and pyramidal cells previously assigned. The cells comprising β will have had their synapses (from the cells comprising α) increased during learning. Thus, if α is presented again, the cells of β will have the highest synaptic input summations in their respective WTA modules. In this case, winners should be chosen on the deterministic basis of these summations: no noise should be present in the winner selection process. On the other hand, increasingly novel inputs should be assigned to increasingly distinct codes, i.e., codes having progressively smaller intersection with existing codes. This can be achieved by increasing the noisiness of the winner selection process in each WTA module, which can be achieved by suppressing the influence of the deterministic synaptic inputs (which reflect prior learning) relative to baseline random (spontaneous) activity. By adjusting parameters that control the global (i.e., across the whole macrocolumn) noise level, we can modulate the expected intersection between the set of cells which have the maximal input summations in their respective WTA modules and the set of winners that are actually chosen, thus implementing SISC.

Many experimental and theoretical studies implicate neuromodulators, notably norepinephrine (NE) and acetylcholine (ACh), in functionality similar to the above, which can be described generally as modulating signal-to-noise ratio (SNR). Doya (2002) proposed that NE levels control the amount of noise in a process of choosing output actions. However, Doya’s model assumes a localist representation of the choices, which precludes possession of the SISC property (see Discussion). In addition, increased ACh has been shown to selectively increase the strength of afferent relative to intrinsic inputs in piriform cortex (Hasselmo and Bower, 1992) and other brain structures (see Hasselmo, 2006 for review). These ACh findings have been summarized as showing that increased ACh adjusts network dynamics to favor encoding new memories compared to retrieving old memories, which fits well with the proposed CSA functionality. Following the model description, I offer a speculative mapping of my proposed model onto neural circuitry and discuss evidence for novelty-contingent noise modulation by both NE and ACh. However, the specifics of this mechanism are a subject of ongoing research and likely will involve interactions between neuromodulatory systems (cf. Briand et al., 2007).

Any discussion of columnar function of course centrally concerns cortical circuitry, and more specifically, the putative canonical cortical microcircuit (Rockland and Pandya, 1979; Douglas et al., 1989; Douglas and Martin, 1991). I therefore want to finish the Introduction with the following point. We have made huge progress in understanding many of the components of cortical microcircuitry – a tiny sample of which includes (DeFelipe et al., 1990; Larkum et al., 2001; Beierlein et al., 2003; Schubert et al., 2003; Zhu et al., 2004; Feldmeyer et al., 2006; Fukuda et al., 2006; Krieger et al., 2007; Egger et al., 2008; Hirata and Castro-Alamancos, 2008; Berger et al., 2009; Murayama et al., 2009; Symes and Wennekers, 2009; Briggs, 2010; and see Thomson et al., 2002; Bannister, 2005; Silberberg et al., 2005 for reviews). Nevertheless, we remain far from any sort of comprehensive and consensual understanding of how cortical columnar circuitry manipulates, i.e., stores and retrieves, specific items of information. In the main, only very broad conclusions regarding information processing are asserted in the experimental literature, e.g., horizontal connections between fast-spiking L4 interneurons and pyramidal cells involved in formation of L4 assemblies and sharpening of tuning (Sun et al., 2006); that both the populations of L4 pyramids and of L5A pyramids have transcolumnar connectivity patterns allowing them to act as integrators of information coming in from multiple vibrissae in parallel, or in close sequence (Schubert et al., 2007); that the receptive fields of barrel-related L2/3 pyramids are dynamic and thus may reflect learning to recognize spatiotemporal patterns of vibrissae deflections (Brecht et al., 2003); that WTA competition occurs in the supra- and infragranular layers (Douglas and Martin, 2004); and that local (~100 µm) L2/3-to-L2/3 connections might serve to synchronize firing of L2/3 cell assemblies (Lübke and Feldmeyer, 2007); etc. I believe the hypothetical model described herein to be a significant contribution because it goes beyond broad conclusions and offers a mechanistic explanation of how specific informational items are learned and retrieved and in so doing, proposes a generic function for the minicolumn, i.e., that it functions as a WTA module in support of manipulating SDCs at the next higher, i.e., macrocolumnar, scale.

RESULTS: MODEL DESCRIPTION

Figure 2 shows the functional architecture of a simplified version of the model. In particular, it was stated in the Introduction that sparse macrocolumnar codes are chosen in response to a macrocolumn’s overall input, which includes its BU, H, and TD inputs. However, illustrations of the model in operation in that general case become rather complex, particularly since the H (and TD) weights carry temporal information, which necessitates showing the model at multiple successive time steps while processing spatiotemporal patterns. More importantly, the core elements of the hypothesis – which are: (a) that the macrocolumn stores SDCs consisting of one winning L2/3 cell per minicolumn; and (b) that the SISC property is achieved by modulating the amount of randomness (noise) present in the winner selection process in inverse proportion to input familiarity – can be clearly and more simply described for the BU-only case (i.e., where inputs are purely spatial patterns). Therefore, the model description in this paper will be limited to the BU-only case. However, the generalized model (with BU, H, and TD inputs) and the accompanying generalized version of the CSA are given in Figures S2 and Table S1 in Supplementary Material.

In Figure 2, the input field, F1, is comprised of 12 binary units and can be considered analogous to a specific thalamic nucleus, though topographical organization is not assumed. The coding field, F2, consists of Q = 4 WTA CMs, each containing K = 3 binary units. Complete (all-to-all) BU connectivity from F1 to F2 is assumed for simplicity. These BU weights (synapses) are binary, initially 0, and are permanently set to a weight of 1 the first time the pre- and postsynaptic units are co-active (i.e., Hebbian learning).

MODEL DYNAMICS: THE CODE SELECTION ALGORITHM

The model’s core algorithm, the CSA, determines which cells are chosen to represent an input, during both learning and retrieval. A single iteration of the algorithm involves two rounds of competition in the CMs of F2. The first round is a hard WTA competition (represented by boxes labeled “Max” in Figure 2). The purpose of the first round is to compute a global familiarity measure, G, of the input pattern. G then drives a global modulation of the F2 unit...
activation function (Figure 2: purple arrows) in preparation for
the second competitive round, which is a soft WTA competition,
the intent of which is that:

1. as $G$ goes to 1 (indicating a completely familiar input), the pro-
bability that the unit with the highest input summation in a
CM wins approaches 1, and

2. as $G$ goes to 0 (indicating a completely novel input), all units
in a CM become equally likely to win (regardless of their input
summations).

This policy ensures, statistically, the SISC property. The steps of
the CSA are as follows.

1. Each F2 unit $i$ computes its raw input summation, $u(i)$.
$$u(i) = \sum_{j \in \alpha_n} w(j,i)$$
where $\alpha_n$ is the current input (F1) pattern. Because unit activa-
tions are binary, we can simply sum the weights, $w(j,i)$, which
are also binary.

2. Normalize $u(i)$ to $[0..1]$, yielding $V(i)$.
$$V(i) = u(i)/S$$
where $S$ is the number of active units in the input pattern. $V(i)$ is a local
measure of support, or likelihood, that F2 unit $i$ should be acti-
vated. It reflects how well unit $i$’s receptive field (RF), specified
by its afferent weight vector, matches the current input vector.

3. (Round 1 competition) The maximum $V(i)$, $\hat{V}_X$, is found in
each of the Q CMs.
$$\hat{V}_X = \max_{i \in C_x} \{V(i)\}$$
where $x$ indexes the CMs and $i$ indexes the units in a CM, $C_x$.

4. Average the $Q \hat{V}_X$ values, yielding $G$, a global measure of the
familiarity of the current input.
$$G = \frac{\sum_{x=1}^{Q} \hat{V}_X}{Q}$$

5. The expansivity, $\eta$, of the probabilistic activation function
(which is implemented via steps 6–8) is set as an increasing
nonlinear function of $G$ (Eq. 5, expressed as a table).

\begin{align*}
G &\quad 0.0 & 0.2 & 0.4 & 0.6 & 0.8 & 1.0 \\
\eta &\quad 0 & 0 & 0.2 & 5 & 12 & 100
\end{align*}

$\eta$ corresponds to sigmoid height (in Eq. 6). The idea is to increase
the range of relative win likelihoods, $\psi(i)$ (defined in step 6) over
any given CM’s units as $G$ goes to 1. This in turn, serves to non-
linearly exaggerate the difference in the final win probabilities
(Eq. 7) between F2 units with low and high $V$ values. The specific
parameters of any instance of the $G$-to-$\eta$ mapping will determine
the specifics of the relation between input similarity and code
similarity, i.e., the expected code intersection as a function of
input similarity. The specific $\eta$ values in Eq. 5 were chosen to
yield the $p$-distributions in the examples of Figures 3 and 4.

6. The $V$ values of all units in all CMs are then passed through
the sigmoidal activation function (Eq. 6) whose shapeSCALE
reflects $G$. Again, particular parameter values affect the
relation of input similarity to code similarity (and there-
fore, storage capacity); values of $\lambda = 28$ and $\phi = -5$ produce
the $V$-to-$\psi$ mappings in Figure 4. As noted above, within
each CM, the output variable, $\psi(i)$, can be viewed as a rela-
tive likelihood that unit $i$ should be chosen winner. The
$\psi$-distributions in each CM are normalized to final proba-
bilities in step 7.
\[ \psi(i) = \frac{\eta}{1 + e^{-(\lambda V(i) + \phi)}} + 1 \]

When \( G = 1 \) (perfectly familiar), \( \eta \) is maximized (in Eq. 5), which maximizes relative and total (once normalized, via Eq. 7) probabilities of winning for units with the maximum \( V \) value in their respective CMs. In contrast, when \( G = 0 \) (completely novel), \( \eta = 0 \), which collapses the sigmoid to the constant function, \( \psi = 1 \), thus making all units in a CM equally likely to win. This causes the expected intersection of the code being chosen in the current instance with any previously assigned code to be at chance level. In general, this modulation of the sigmoid activation function tends toward code completion in proportion to the familiarity of the input and code separation in proportion to its novelty.

7. Transform relative likelihood distribution (\( \psi \)) in each CM to true probability distribution (\( \rho \)).

\[ \rho(i) = \frac{\psi(i)}{\sum_{k \in \text{CM}} \psi(k)} \]

8. (Round 2 competition) Choose an F2 code by drawing a winner from the \( \rho \)-distribution (soft max) in each CM. Thus, choosing an F2 code is actually performed as \( Q \) separate draws. When \( G = 0 \), these draws are statistically independent, as in Figures 3 and 4D. As we consider increasingly familiar inputs, i.e., for \( G \) approaching 1 (and, assuming the model is still operating in a regime where crosstalk is sufficiently low), the draws become increasingly correlated (dependent), as can be seen in going from Figure 4C to 4B to 4A.

**Figure 3** graphically illustrates the operation of the CSA in the case of the model being presented with its first input, \( \alpha_1 \). The gray arrows indicate that the BU signals propagating from the active F1 units will be traversing connections with zero synaptic strength. This leads to unnormalized (\( u \)) and normalized (\( V \)) input summations of 0 for all 12 F2 units (steps 1, 2). In step 3, the max \( \hat{V} \), \( \hat{V}_i \), in each CM is found (ties broken at random). In step 4, \( G \) is computed as the average of the \( \hat{V} \) values: in this case all the \( \hat{V} \) are 0, so \( G = 0 \). In step 5, the value, \( G = 0 \), maps to \( \eta = 0 \), which causes the activation function of the F2 units to collapse to the constant function, \( \psi = 1 \). In step 6, each F2 unit applies this activation function to its \( V \) value, yielding the uniform relative likelihood distribution in each CM. In step 7, the relative likelihood function in each CM is normalized to a true probability (\( \rho \)) distribution, which in this case, is again uniform. Finally, in step 8, a winner is drawn in each CM, resulting in a random F2 code, e.g., \( \beta_1 \).
**Figure 4** demonstrates that the CSA realizes the SISC property by considering four possibilities (A–D) for the second input presented to the model of **Figure 3**. These four inputs, $\alpha_2$–$\alpha_5$, range from being identical to $\alpha_1$ (completely familiar) to having zero overlap with $\alpha_1$ (completely unfamiliar). To save space, the panels of **Figure 4** use an abbreviated version of the format of **Figure 3**. Most noticeably, the intermediate variable, $\psi$ (relative likelihood), is not shown. However, the transform from $V$ through to $\rho$ should still be clear. Black BU connections are ones that were increased to one when $\alpha_1$ was learned (**Figure 3**). The overall message of **Figure 4** is as follows. Working from **Figure 4A** to **4D**, the inputs have progressively lower similarity (intersection) with $\alpha_1$: F1 units not in common with $\alpha_1$ are shown in green. As $G$ drops, the sigmoid expansivity drops (note the changing $\psi$ scale). Thus, the $\rho$-distributions become progressively flatter, which in turn results in F2 codes, $\beta_2$–$\beta_5$, having progressively smaller intersection with $\beta_1$. F2 units not in common with $\beta_1$ also shown in green.

**Figure 4A** shows the case of presenting a completely familiar input again, and is thus a recognition test trial, demonstrating retrieval. This leads, via CSA steps 3 and 4, to $G = 1$, which yields, via steps 5 and 6, the expansive nonlinear $V$-to-$\psi$ mapping shown (red sigmoid). This nonlinearity is applied to every F2 unit, yielding the highly peaked $\rho$-distributions shown. Finally, one unit is drawn in each CM. The probability of drawing the correct unit in any single CM is approximately 98%. Of course, what’s crucial in this case, i.e., when the input is completely familiar ($G = 1$), is that the entire correct F2 code is reactivated. In this case, that probability is $(0.98)^4 \approx 92\%$. Thus, the familiarity, $G$, which depends on the entire F2 layer and is thus global information, influences...
the local activation functions so as to produce the desired overall result, in this case, reactivation of the code (memory trace), \( \beta \), of the familiar input pattern, \( \alpha \). The explanations of the remaining panels follow that of Figures 3 and 4A. In going from Figure 4B to 4D, one can readily see decreasing intersection with \( \alpha \), decreasing \( \alpha \) and \( \eta \) values, decreasing \( G \), decreasing sigmoid expansivity, progressively flatter \( \rho \)-distributions, and ultimately, decreasing intersection with \( \beta \).

Given a desired probability, \( R \), of correctly reactivating an entire code (i.e., of choosing the correct unit in each CM), when \( G = 1 \), given values for \( Q \) and \( K \), we could compute the needed value of \( \eta \). However, the macrocolumn is a content-addressable associative memory and in actual usage, multiple sparse codes will be stored in superposition. Any thorough analysis of the model’s expected retrieval error must include the effect of overlap between the stored codes (i.e., cross-talk): this influences the shapes of the \( \rho \)-distributions and thus, the expected retrieval accuracy for any given number of stored codes. Such an analysis will be conducted empirically and reported in a separate paper.

Before leaving Figure 4, I underscore three important points. First, while the \( \rho \)-distributions become flatter as \( G \) decreases, the units comprising the code of the most similar previously learned input (here, \( \alpha \)) remain most likely to win in their respective CMs. If we simply deterministically chose the unit with maximum \( V(i) \) in each CM, we would have chosen the same F2 code, \( \beta \), in response to all four inputs, \( \alpha = \alpha \). Thus, the computation of a quantity, \( G \), which depends on all the CMs is essential to achieving the SISC property. It constitutes a channel through which information transfers between all F2 units throughout the whole macrocolumn. As noted earlier, the full model also assumes direct “H” connections between F2 units, analogous to the horizontal matrix of L2/3 (see Figure S2 in Supplementary Material). These also mediate communication, but of the prior code active in the macrocolumn, not of the simultaneous state of all F2 units throughout the macrocolumn.

Second, learning is single-trial and involves only one iteration of the CSA. This is largely facilitated by the fact that when a given input-code association, \( \alpha \rightarrow \beta \), is learned, each of \( \beta \)’s F2 units simultaneously has its afferent weight from all of \( \alpha \)’s F1 units increased. The effect of these simultaneous correlated potentiations allows a rapid, even single-trial, formation of an association, even if the individual synaptic potentiations are small, consistent with the recent characterization of thalamocortical learning described in Bruno and Sakmann (2006).

Third, Figure 4A shows that recognizing an exact instance of a previous input also requires only one iteration of the CSA. Although this example does not directly show it, this holds for recognition of non-exact matches as well. Evidence for this will be presented in a separate work. That both learning and recognition require only a single CSA iteration is especially significant since, as can readily be seen, none of the CSA steps involves iterations over stored codes: thus, the time it takes for the CSA to either store a new input or retrieve the closest matching stored input remains constant as the number of stored codes increases. This does not imply that an infinite number of codes can be stored: of course, the model has finite storage capacity. This capacity will be characterized in future research, but should be similar to other sparse associative memories (Willshaw et al., 1969; Palm, 1982; Moll and Miikkulainen, 1995; Knoblauch et al., 2010).

PROSPECTIVE MAPPING TO CORTICAL CIRCUITRY

There remain huge gaps in our knowledge of the intrinsic physiological, synaptic, morphological, and connectional properties of all classes of cortical cell and of functional relationships between cortical and sub-cortical structures. Nevertheless, Figure 5 shows a possible neural realization of the model’s WTA CM, i.e., minicolumn, and dynamics (CSA). I have attempted to respect known constraints but the realization is admittedly speculative and ongoing modifications will undoubtedly be required. Figures 5A–E show the critical events transpiring in a single minicolumn at five points in time during the CSA’s computational cycle. Note that due to space limitations Figure 5 cannot depict the true extents of the various axonal and dendritic systems of the cells involved. Figure S3 in Supplementary Material provides a more global context showing these extents.

Figure 5A shows the initial CSA steps 1 and 2 when the L2/3 pyramidal (here only two cells, but in reality, ~20) integrate their inputs. While the CSA explanation in the prior section included only the BU inputs, all three input classes are included here:

- BU inputs (labeled “2”) are mediated via L4 (Rockland and Pandya, 1979)
- TD inputs (“1”) are mediated via L2/3 apical tufts (Rockland and Drash, 1996)
- H inputs (“3”) are mediated via the horizontal matrix of L2/3 (Gilbert and Wiesel, 1989; Feldmeyer et al., 2006)

All three input vectors arrive in parallel and collectively give rise to postsynaptic potentials (PSPs) in the L2/3 pyramids. The three (normalized) inputs are combined multiplicatively; see the generalized version of the CSA (Table S1 in Supplementary Material). The chandelier cells (represented by a single red unit labeled “C”) are firing at this time, preventing the L2/3 pyramids from firing.

In Figure 5B, the chandeliers shut off (grayed out) and the L2/3 pyramid with the highest PSP (cell 2) is assumed to be the first to spike (CSA step 3). This winning cell, and more specifically, its PSP value (\( V \) in Eq. 2), represents this minicolumn’s local judgment of how similar the macrocolumn’s closest-matching stored input is to the current overall (i.e., BU, H, and TD) input. The output of cell 2 is then communicated to some locus where it is averaged with the round 1 winners from the other ~70 minicolumns of the macrocolumn, yielding \( G \) (CSA step 4). As noted in the Introduction, the functionality related to \( G \) seems most consistent with the phenomenology of neuromodulatory systems, especially ACh and NE. Support for this speculation is given in the following sub-section. Note that the communication of cell 2’s PSP value is hypothesized to be mediated via L5, one of whose pyramidal cells is seen integrating here (light green); this is based loosely on evidence that L5 cells, specifically L5B pyramids, almost exclusively target pontine areas (with collaterals to thalamus) (Deschênes et al., 1994; Krieger et al., 2007).

L2/3 pyramids are the primary source of BU signals to higher cortical areas (Rockland and Pandya, 1979; and see Thomson et al., 2002; Brecht et al., 2003; Schubert et al., 2003; Bannister, 2005;
Helmstaedter et al., 2007; Lübke and Feldmeyer, 2007; Petersen, 2007; Egger et al., 2008; Lefort et al., 2009 for wider background on cortical columnar circuitry relevant to the current proposal). In addition, as stated earlier, the horizontal L2/3-to-L2/3 connections are proposed to communicate this macrocolumn’s final hypothesis regarding its total input pattern in the current CSA cycle recurrently back to the same (and surrounding) macrocolumns on the next CSA cycle. Hence, it is crucial that since that final hypothesis is not present until the second round of competition completes (Figure 5E), the output pathways carrying those signals must be closed (red “x”s on paths “4” and “5”). Though not depicted here, one possible mechanism for selectively preventing horizontal signaling in L2/3 is activation of the double bouquet cells (DeFelipe et al., 1990, 2006; Peters and Sethares, 1997). Their “horsetail” axons, being interdigitated, nearly one-to-one with minicolumns would allow them to make contact with a substantial portion of the horizontally (and obliquely) oriented dendritic and axonal processes, in L2/3, and thus prevent passage of horizontal signals.

In Figure 5C, the L5 pyramidal mediating the winning L2/3 cell’s PSP value has reached threshold and sends that output to the sub-cortical averaging locus (path “6”). In addition, the winning cell itself has activated the local basket cell network (electrically coupled, cf. Brown and Hestrin, 2009), represented by the unit labeled “B”, which rapidly deactivates and re-polarizes (resets) the L2/3 pyramids (grayed out). This reset need not be back to a completely even baseline: some remnant of the relative PSP distribution prior to basket cell activation might remain, biasing the second round of competition.

In Figure 5D, the result of the subcortical computation of $G$ is returned to the macrocolumn (path “7”) in the form of neuromodulator release (purple cloud surrounding the L2/3 pyramids). This release modifies the activation functions of the L2/3 pyramids, as described earlier. Note that this neuromodulatory “cloud” actually extends across a broad, i.e., macrocolumnar (or wider), expanse of L2/3, not just within a single minicolumn as this figure may suggest. The chandeliers are again firing to prevent any L2/3 from firing as the second round of integration occurs. The basket cells are inactive, allowing this integration to take place.

In Figure 5E, the chandeliers again deactivate. The L2/3 pyramidal with the highest PSP is the first to spike. In general, the pyramidal cell winning on this second round of competition may differ from the first round winner. In particular, the probability that the second round winner is the same as the first round winner increases with $G$. The set of L2/3 winners, one per minicolumn, across the whole macrocolumn represents that macrocolumn’s final decision (hypothesis) as to identity of its current overall (TD, H, and BU) input. Thus, the output of the winning L2/3 cell in each minicolumn is now communicated to:

1. Lower cortical regions via L5 and its backprojections to the lower regions’ L1 (labeled “8”) (Rockland and Drash, 1996).
2. L2/3 pyramids in the same and neighboring macrocolumns via the local horizontal L2/3 matrix (“5”) (Gilbert and Wiesel, 1989; Feldmeyer et al., 2006), thus delivering temporal context information (recurrently) to the local region to be integrated on the next CSA cycle.
3. The L4 layer of higher cortical regions (“4”) (Rockland and Pandya, 1979).
Note that the output of the winning L2/3 cell should be prevented from recurring to the local basket network at this time so as to allow the integration period to occur at the beginning of the next computational cycle; hence, the red “x” on the link to basket cell.

I reiterate that the above possible cortical realization of the proposed SDC model is highly speculative. It clearly lacks numerous details, especially regarding processing in the intermediate processing stages, e.g., L4, and output processing involving L5 (and L6). Nevertheless, it is a starting point and can be falsified, especially as experimental methods mature. For example, the many timing relationships in the circuit can be tested. We still have decidedly little in the way of hard constraints on the time courses of activation of the many cell types involved in cortical (and hippocampal) circuits, though progress is being made (Klausberger et al., 2003, 2004; Silberberg et al., 2005; Silberberg and Markram, 2007; Klausberger and Somogyi, 2008; Otsuka and Kawaguchi, 2009; Woodruff et al., 2009).

Moreover, the proposed theory’s key assumption that the L2/3 pyramidal cells are the core repository of information in cortex and that the codes laid down in L2/3 are the context-dependent memories of our experiences, is subject to challenge. Specifically, the anatomy of the L5 thick tufted cells suggests that they too have access to BU (via L4), TD (via their apical tufts in L1), and H (via an extensive intra-L5 horizontal network, Schubert et al., 2007) inputs, and therefore that L5 might store the most detailed and context-dependent codes in cortex, a view supported by findings such as (de Kock et al., 2007). In the end, for the purpose of this “hypothesis and theory” paper, I believe the architecture and algorithm (CSA) to be more important than the specifics of any particular neural realization.

Support for neuromodulator-based implementation of familiarity-contingent noise

In this section, I consider evidence relating to six model predictions:

a) *Signals generated in the macrocolumn [i.e., the $V^*$ (Eq. 3)] can influence neuromodulatory systems (brown links in Figure 2).* Strictly interpreted, Figure 2 suggests that the model can only be true of cortical areas that have direct projections to the activation function modulator (AFM), hypothesized to be instantiated in midbrain neuromodulator source areas, e.g., basal forebrain (BF, source of ACh) and locus coeruleus (LC, source of NE). Relatively few cortical areas project directly to BF or LC. Direct cortical afferents to BF arise mainly from prepyriform, anterior insula, orbitofrontal, entorhinal and medial temporal areas (Mesulam and Mufson, 1984). Direct cortical afferents to LC arise from dorsal prefrontal cortex (Arnsten and Goldman-Rakic, 1984), medial prefrontal cortex (Jodo et al., 1998). While direct projections are limited, a much larger fraction of cortex may be able to influence the hypothesized AFM via multi-synaptic pathways involving thalamus and other subcortical structures, especially via pathways interconnecting BF, LC, and other neuromodulator source areas. For example, BF cholinergic neurons are excited by LC (Jones et al., 2004), which allows dorsal and medial prefrontal areas indirect influence on BF. Similarly, LC receives input from the Raphe nuclei (reviewed in Samuels and Szabadi, 2008) which would allow further extension of the sphere of cortical influence upon the AFM.

This is a subject of ongoing research. However, it is clearly possible that my macrocolumnar model applies only to the smaller set of cortical areas suggested above. There is some merit to this idea. After all, there would be some advantage to deferring the decision as to the overall familiarity/novelty of the current input (moment) to the very highest cortical levels, which are in position to make the most informed decisions. In this case, once G is computed, it is then broadcast pan-cortically, i.e., to all levels of the hierarchy, allowing the local choice of code to proceed accordingly, i.e., with a level of randomness appropriate to G.

b) *There exists some neuromodulatory signal, $\eta$ (Eq. 5), which correlates with the detection of familiarity, and/or inversely with the detection of novelty.* Such correlations have been shown for both ACh (Miranda et al., 2000, 2003) and NE (Sara et al., 1994; Vankov et al., 1995).

c) The signal $\eta$ can physically reach cortex (purple arrows in Figure 2). LC projects to all of cortex (Foote and Morrison, 1987; Berridge and Waterhouse, 2003; Samuels and Szabadi, 2008). BF projects to almost all cortical areas (reviewed in Briand et al., 2007). The amount of randomness to be added to the winner selection process is a global parameter, which applies non-specifically to all the minicolumns. This is consistent with volume transmission believed to be used by neuromodulatory systems (Descarries et al., 1997; see Sarter et al., 2009 for discussion of the complexities of the evidence regarding volume transmission).

d) *The signal $\eta$ determines (Eqs 6–8) the amount of noise (randomness) in the selection (activation) of cortical (i.e., macrocolumnar) codes.* Controlling the noisiness of a process of choosing a winner from a competing group of neurons can be achieved by some combination of two actions: (i) increasing the spike probability of cells with high input summations relative to those with low summations and (ii) lowering the spike probability of low-input cells relative to high-input cells. Both of these actions can be achieved by uniformly (i.e., to all competing cells in a WTA module) modulating intrinsic cell properties such as excitability. Numerous studies have demonstrated both excitatory and suppressive effects on target cell responses (both principal neurons and interneurons) for both ACh (Kawasaki and Avoli, 1996; Shalinsky et al., 2002; Cobb and Davies, 2005; Tateno et al., 2005; Isakova and Mednikova, 2007; Lawrence, 2008; Eggermann and Feldmeyer, 2009) and NE (Foote et al., 1975; Kawaguchi and Shindou, 1996; Harly and Helen, 2007; Moxon et al., 2007). It is not my intention here to argue for a precise realization of this mechanism. As suggested in many reviews (Berridge and Waterhouse, 2003; Lucas-Meunier et al., 2003; Sara, 2009), the landscape of this research is very complex and we are far from a comprehensive understanding of how the various neuromodulatory systems affect high-level cognitive processing either alone or in concert (Briand et al., 2007). Nevertheless, the large and varied body of evidence at least admits the possibility that one or more of these neuromodulators could implement the familiarity-contingent AFM mechanism (CSA steps 5–8; see Doya, 2002, p. 502, for similar speculation).
e] Decreased $\eta$, i.e., increased noise, leads to greater code separation (decreased intersection). Recently, Goard and Dan (2009) showed that increased BF stimulation decreased the correlation amongst a population of rat V1 cells. This decreased correlation essentially shows increased separation between population codes, which in the model proposed here, would manifest as decreased intersection between sparse codes.

f] Disabling of the brain's ability to produce high noise, i.e., causing $\eta$ to be permanently high, should reduce the ability to learn new inputs, while sparing or having much less effect on recognition of known items. Looking at Figure 4, if the AFM was “stuck” in the highly expansive sigmoid condition (low noise), all four inputs, $\alpha_2$-$\alpha_n$, would have high probability of mapping to the same code, $\beta$. This would prevent the model from being able to distinguish them in future presentations. However, in general, inputs that were mapped to unique codes prior to such a disabling event will reliably activate those codes on future presentations. In accord with this, Browning et al. (2010) found that severely diminishing cholinergic inputs to inferotemporal cortex severely reduced macaques’ performance on a visual episodic memory task, while having little effect on a DNMS task. McGaughy et al. (2005) found a similar effect: cholinergic deafferentation of entorhinal cortex reduced performance on DNMS tasks involving novel odors but not familiar odors.

DISCUSSION

I have described a theoretical model of cortical function that explains the functional relationship between the minicolumn and macrocolumn. Specifically:

a] The macrocolumn (in any of its forms) is proposed to store information in the form of SDCs, and

b] The minicolumn (specifically, its L2/3 pool of pyramidalis) is proposed to operate as a WTA CM, the purpose of which is to enforce the sparseness of the macrocolumnar code.

Two key motivations for this model are the computational advantages of SDC and the increasingly strong evidence for SDC in the brain, cited in the Section “Introduction”. One important advantage of SDC over a localist code is that the number of unique items that can be stored can be far larger than the number of representing units. For example, the 12 F2 units of the model in Figure 2 allow $3^4 = 81$ unique codes, though in realistic systems, e.g., with less than complete connectivity leading to and from a coding field like F2, the number of those codes that can safely (i.e., while maintaining retrieval error rates below some acceptable criterion) be assigned will be substantially lower than 81. Nevertheless, if the number of input items that will need to be distinguished is not known a priori, SDC is more flexible.

A second computational advantage of SDC is that, if used in conjunction with an appropriate storage/retrieval algorithm it possesses the SISC property. I demonstrated, with the small but statistically reasonable example of Figures 3 and 4, that the CSA yields the SISC property. The SISC property strongly differentiates SDC from localist models: it is not even defined for a localist model since every code is formally disjoint with every other code. Hence, there is no structural way to represent degrees of similarity in a localist code. If there is no way to represent a measure, e.g., similarity, structurally, then whenever that measure is required – e.g., when the closest matching stored item in a database (i.e., macrocolumn) to an input must be returned – it must be computed, which takes time and energy. In contrast, when items’ codes are stored in physically overlapped fashion such that the degree of code overlap represents item similarity, as is the case for the proposed model, the most closely matching stored item will be returned immediately, i.e., without requiring any serial search through the stored items. Figure S4 in Supplementary Material shows test retrievals of the four unique codes stored in the model of Figures 3 and 4, demonstrating possession of this immediate access property for this small example. Empirical proof of this property based on larger scale simulations is currently being developed.

I consider the representation and the CSA to be the most important contributions of this paper because of the computational advantages just described. However, I believe the suggestion that the minicolumn’s generic function is to act as a WTA CM is also important. Saying only that a group of L2/3 units forms a WTA CM places no a priori constraints on what their tuning functions or receptive fields should look like. This is what gives that functionality a chance of being truly generic, i.e., of applying across all areas and species, regardless of the observed tuning profiles of closely neighboring units. Indeed, a recent calcium imaging study of mouse auditory cortex by Rothchild et al. (2010) shows highly heterogeneous small-scale (even immediately adjacent cells) tuning even though the large-scale tuning is tonotopic. Experimental methods are only now just reaching the point where this hypothesis might be directly testable, e.g., modifying calcium imaging methods to have millisecond temporal granularity; see Ohki and Reid (2007).

In a sense, the main point of this paper is that a generic minicolumn function becomes apparent as soon as we postulate that what the cortex, i.e., a macrocolumn, generally does is store and retrieve (access) SDCs of specific context-dependent inputs. As noted in the Section “Introduction”, the experimental literature contains little in the way of proposals linking the formation and retrieval of specific SDCs (i.e., of specific input items, especially of temporal context-dependent items) to the cortical microcircuitry. My proposed model goes beyond broad conclusions and offers a mechanistic explanation of how specific informational items are learned and retrieved and in so doing, proposes a generic function for the minicolumn, i.e., that it functions as a WTA module in support of manipulating SDCs at the next higher, i.e., macrocolumnar, scale.

There have been several recent models linking formation/retrieval of specific items to cortical circuitry and which describe specific roles for the minicolumn (Kupper et al., 2007; George and Hawkins, 2009; Litvak and Ullman, 2009; Schrader et al., 2009). However, all of these models use localist representations and therefore would not possess the advantages of SDC described above. The Cortext model (Kupper et al., 2007; Schrader et al., 2009) assumes that each minicolumn in a hypercolumn represents one particular input feature. On each computational cycle, a WTA process runs within each hypercolumn, such that exactly one minicolumn wins, which would be strongly at odds with the calcium image data (Ohki et al., 2005). A second problem is that the assumption that whole minicolumns compete with each other implies that any given hypercolumn (at any level of the cortical hierarchy) can represent only ~70 unique features (equivalence classes), which seems severely restrictive, especially for hypercolumns at higher cortical levels, e.g., IT.
also postulates that the L2/3 pool of neurons in a minicolumn implements a max function. However, their model proposes that each single minicolumn (specifically, its L2/3 pool) is partitioned into several disjoint groups (“cliques”) of cells, each representing a different item. Since any particular cell can participate in only one clique, this constitutes a localist code. George and Hawkins (2009) also assume that minicolumns represent informational items in a localist fashion. Note however that both George and Hawkins (2009) and Litvak and Ullman (2009) explicitly mention moving to a more general combinatorial code, a.k.a. SDC, as a future research direction.

A core principle of the proposed model is this notion of controlling the amount of noise in the process of choosing (activating) a macocolumnar code as an inverse function of input similarity. Doya (2002) uses the same principle, referred to as “Boltzmann selection”, to modulate the amount of noise in the process of choosing amongst output action actions. Doya specifically hypothesizes that NE controls the noise whereas I can assert only that it is some neuromodulator-based mechanism. In Doya’s model, as NE levels increase, the action with the greatest expected reward is chosen with probability approaching 1. This is suggested as corresponding to the “exploitation” end of the exploitation–exploration continuum. As NE levels drop to 0, all actions become equally probable, i.e., “exploration”, which is appropriate if no single action has a particular high expected reward, which generally correlates with the condition of novelty, i.e., of being in a novel environment wherein it is harder to anticipate the outcome of known actions. The analogy to high expected reward in my model is a highly familiar input (G = 1) in which we want the stored code for that familiar input to be reactivated with probability approaching 1; the condition where no action has a high expected reward is analogous to low familiarity, i.e., where no stored input is very similar to the current input, in which case we want to lay down a new memory trace for the novel input. Despite the similarities, Doya’s model also assumes a localist representation of the choices and, like the other models just mentioned, cannot realize the advantages of SDC.

I have identified several avenues of active and future research at various points in the text and as noted in the previous section, the prospective neural realization is highly speculative and very incomplete. Several additional questions/issues for future research are:

1. Is the current proposal that the L2/3 cells engage in two rounds of competition in each computational (putatively, gamma) cycle plausible?
2. For simplicity, I have described the model in the simplest case of having only one internal coding field (F2) and processing only purely spatial input patterns. However the core model was originally developed for the spatiotemporal pattern (sequence) case (Rinkus, 1996) and was generalized some time ago to have an arbitrarily deep hierarchy of coding fields (Rinkus and Lisman, 2005). See Figure S2 in Supplementary Material. How do these generalized versions of the model map to neural structures?
3. Is there evidence that chandelier cells become active twice as frequently as baskets, as the proposed realization predicts? Is there evidence for the converse?
4. Although not elaborated herein, the proposed mini-/macrocoluminar model is easily generalized to allow substantial overlap between minicolumns (see Figure S5 in Supplementary Material) and multiple winners in a minicolumn on each computational cycle. These degrees of freedom need to be explored.
5. We know of the fast, phasic, time scales of operation for NE (Rajkowski et al., 2004) and DA (Schultz, 1998) and of slightly slower but still phasic mode for ACh (Gulledge and Kawaguchi, 2007), but these have been proposed as signaling other measures besides pure novelty (Redgrave et al., 1999; Boulart and Sara, 2005; Dayan and Yu, 2006). How might all these signals conspire to implement a pure novelty signal?

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SUPPLEMENTARY MATERIAL

The Supplementary Material for this article can be found online at http://www.frontiersin.org/neuroscience/neuroanatomy/paper/10.3389/fnana.2010.00017/

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Conflict of Interest Statement: The author declares that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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